

**Step 5A Graphical Method.** We now show how to construct Table WE7-2.2.

The derivative  $(-dC_A/dt)$  is determined by calculating and plotting  $(-\Delta C_A/\Delta t)$  as a function of time,  $t$ , and then using the equal-area differentiation technique (Appendix A.2) to determine  $(-dC_A/dt)$  as a function of  $C_A$ . First, we calculate the ratio  $(-\Delta C_A/\Delta t)$  from the first two columns of Table WE7-2.2; the result is written in the third column.

We use numerical differentiation to help identify inconsistencies in the data.

TABLE WE7-2.2 PROCESSED DATA

| $t$ (min) | $C_A \times 10^3$ (mol/dm <sup>3</sup> ) | $-\frac{\Delta C_A}{\Delta t} \times 10^4$<br>(mol/dm <sup>3</sup> · min) | $-\frac{dC_A}{dt} \times 10^4$<br>(mol/dm <sup>3</sup> · min) |
|-----------|--|---|---|
| 0         | 50                                       |   | 3.0   |
|           |  | 2.40 <sup>†</sup>   |   |
| 50        | 38                                       |   | 1.86  |
|           |  | 1.48  |   |
| 100       | 30.6                                     |   | 1.2   |
|           |  | 1.00  |   |
| 150       | 25.6                                     |   | 0.8   |
|           |  | 0.68  |   |
| 200       | 22.2                                     |   | 0.5   |
|           |  | 0.54  |   |
| 250       | 19.5                                     |   | 0.47  |
|           |  | 0.42  |   |
| 300       | 17.4                                     |   |   |

$$^{\dagger} -\frac{\Delta C_A}{\Delta t} = -\frac{C_{A2} - C_{A1}}{t_2 - t_1} = -\left(\frac{38 - 50}{50 - 0}\right) \times 10^{-3} = 0.24 \times 10^{-3} = 2.4 \times 10^{-4} \text{ (mol/dm}^3 \cdot \text{min)}$$

Next, we use Table WE7-2.2 to plot the third column as a function of the first column in Figure WE7-1.1 [i.e.,  $(-\Delta C_A/\Delta t)$  vs.  $t$ ]. Using equal-area differentiation, the value of  $(-dC_A/dt)$  is read off the figure (represented by the arrows); then it is used to complete the fourth column of Table WE7-2.2.

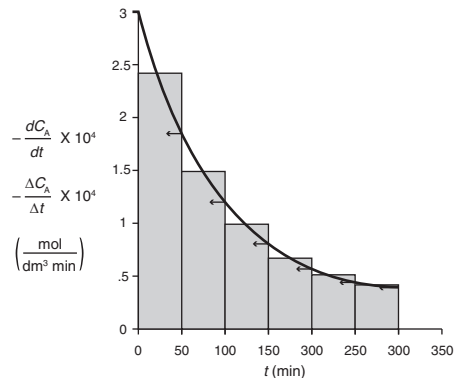


Figure WE7-2.1 Graphical differentiation.

The results to find  $(-dC_A/dt)$  at each time,  $t$ , and concentration,  $C_A$ , are summarized in Table WE7-2.2.